

Simultaneous equations

1. Solve the simultaneous equations.

$$\begin{array}{lll} 5x + 3y = 22 \times 2 & 10x + 6y = 44 & A \\ 2x + 4y = 20 \times 5 & 10x + 20y = 100 & B \end{array}$$

Do not use trial and improvement.

$$\begin{array}{l} B - A \quad 14y = 56 \\ y = 4 \end{array}$$

$$\begin{array}{l} 5x + 3(4) = 22 \\ x = 2 \end{array}$$

(3 marks)

2. Solve the simultaneous equations

$$\begin{array}{lll} 4x - 4y = 8 \times 3 & 12x - 12y = 24 & A \\ 5x - 3y = 18 \times 4 & 20x - 12y = 72 & B \end{array}$$

Do not use trial and improvement.

$$\begin{array}{l} B - A \quad 8x = 48 \\ x = 6 \end{array}$$

$$\begin{array}{l} 5(6) - 3y = 18 \\ y = 4 \end{array}$$

(3 marks)

Simultaneous equations

3. Solve the simultaneous equations

$$5x - 6y = 28 \times 2 \quad 10x - 12y = 56 \quad A$$

$$4x - 4y = 24 \times 3 \quad 12x - 12y = 72 \quad B$$

Do not use trial and improvement.

$$B - A \quad 2x = 16$$

$$x = 8$$

$$5(8) - 6y = 28$$

$$y = 2$$

(3 marks)

4. Solve the simultaneous equations

$$6a + 2b = -2 \times 3 \quad 18a + 6b = -6 \quad A$$

$$4a - 3b = 29 \times 2 \quad 8a - 6b = 58 \quad B$$

Do not use trial and improvement.

$$B + A \quad 26a = 52$$

$$a = 2$$

$$6(2) + 2b = -2$$

$$b = -7$$

(3 marks)

Simultaneous equations

5. Solve the simultaneous equations

$$10x - 6y = 66 \times 3 \quad 30x - 18y = 198 \quad \text{A}$$

$$3x - 9y = 63 \times 2 \quad 6x - 18y = 126 \quad \text{B}$$

Do not use trial and improvement.

$$\begin{aligned} A - B \quad 24x &= 72 \\ x &= 3 \end{aligned}$$

$$\begin{aligned} 10(3) - 6y &= 66 \\ y &= -6 \end{aligned}$$

(3 marks)

6. Solve the simultaneous equations

$$4c + 2d = -14 \times 6 \quad 24c + 12d = -84 \quad \text{A}$$

$$3c - 12d = 30 \times 1 \quad 3c - 12d = 30 \quad \text{B}$$

Do not use trial and improvement.

$$\begin{aligned} A + B \quad 27c &= -54 \\ c &= -2 \end{aligned}$$

$$\begin{aligned} 4(-2) + 2d &= -14 \\ d &= -3 \end{aligned}$$

(3 marks)

Simultaneous equations

7. Solve the simultaneous equations

$$10x - 15y = 25 \quad \times 1 \quad 10x - 15y = 25 \quad A$$

$$x - 2y = 1 \quad \times 10 \quad 10x - 20y = 10 \quad B$$

Do not use trial and improvement.

$$A - B \quad 5y = 15$$

$$y = 3$$

$$x - 2(3) = 1$$

$$x = 7$$

(3 marks)

8. Solve the simultaneous equations

$$2x - 8 = 2y \quad 2x - 2y = 8 \quad \times 1 \quad 2x - 2y = 8 \quad A$$

$$x + 3y = 12 \quad \times 2 \quad 2x + 6y = 24 \quad B$$

Do not use trial and improvement.

$$A - B \quad -8y = -16$$

$$y = 2$$

$$x + 3(2) = 12$$

$$x = 6$$

(4 marks)

Simultaneous equations

9. Solve the simultaneous equations

$$\begin{array}{rclcl} x + 3y = 2 & & \times 2 & & 2x + 6y = 4 & A \\ 2x = 4y + 24 & 2x - 4y = 24 & \times 2 & & 2x - 4y = 24 & B \end{array}$$

Do not use trial and improvement.

$$\begin{array}{rcl} A - B & & 10y = -20 \\ & & y = -2 \end{array}$$

$$\begin{array}{rcl} x + 3(-2) = 2 \\ x = 8 \end{array}$$

(4 marks)

10. The cost of buying 3 adult tickets and 8 child tickets at the theatre is £97.
 The cost of buying 2 adult tickets and 4 child tickets at the theatre is £58.
 Work out the total cost of 2 adult tickets and 1 child ticket.

$$\begin{array}{rclcl} 3a + 8c = 97 & \times 2 & 6a + 16c = 194 & A \\ 2a + 4c = 58 & \times 3 & 6a + 12c = 174 & B \end{array}$$

$$\begin{array}{rcl} A - B & & 4c = 20 \\ & & c = 5 \end{array}$$

$$\begin{array}{rcl} 3a + 8(5) = 97 \\ a = 19 \end{array}$$

$$\text{Total: } 19 + 19 + 5 = \text{£}43$$

(4 marks)

Simultaneous equations

11. The cost of buying 4 plates and 2 cups is £34.
 The cost of buying 3 plates and 1 cup is £21.
 Work out the total cost of 4 plates and 4 cups.

$$\begin{array}{ll} 4p + 2c = 34 \times 1 & 4p + 2c = 34 \quad \mathbf{A} \\ 3p + c = 21 \times 2 & 6p + 2c = 42 \quad \mathbf{B} \end{array}$$

$$\begin{array}{l} B - A \quad 2p = 20 \\ p = 4 \end{array}$$

$$\begin{array}{l} 3(4) + c = 21 \\ c = 9 \end{array}$$

$$\text{Total: } (4 \times 4) + (9 \times 4) = \text{£52}$$

(4 marks)

12. Sarah wants to buy some fruit.
 She buys 5 bananas and 3 apples for £2.25.
 She buys 3 bananas and 7 apples for £3.17.
 Work out the cost of a banana and an apple.

$$\begin{array}{ll} 5b + 3a = 2.25 \times 7 & 35b + 21a = 15.75 \quad \mathbf{A} \\ 3b + 7a = 3.17 \times 3 & 9b + 21a = 9.51 \quad \mathbf{B} \end{array}$$

$$\begin{array}{l} A - B \quad 26b = 6.24 \\ \text{banana} = \text{£0.24} \end{array}$$

$$\begin{array}{l} 3(0.24) + 7a = 3.17 \\ \text{apple} = \text{£0.35} \end{array}$$

(4 marks)

Simultaneous equations

13. Phillip wants to buy some stationary for school.
 He buys 8 pens and 5 pencils for £3.41.
 She buys 9 pens and 2 pencils for £3.22.
 Work out the cost of a pen and a pencil.

$$\begin{array}{ll} 8p + 5c = 3.41 \times 2 & 16p + 10c = 6.82 \quad A \\ 9p + 2c = 3.22 \times 5 & 45p + 10c = 16.10 \quad B \end{array}$$

$$\begin{array}{l} B - A \quad 29p = 9.28 \\ \text{pen} = £0.32 \end{array}$$

$$\begin{array}{l} 8(0.32) + 5c = 3.41 \\ c(\text{pencil}) = £0.17 \end{array}$$

$$\text{Total: } (4 \times 4) + (9 \times 4) = £52$$

(4 marks)